



Introductory Chemistry I

MASS, MOLES, & CONCENTRATIONS

NUMBER OF MOLES OF A

$$n_A = \frac{\text{Mass, } m_A}{\text{Molar mass, } M_A} = \frac{\# \text{ of particles}}{6.022 \times 10^{23}}$$

MOLE FRACTION OF A

$$X_A = \frac{\text{Moles of A}}{\text{Total moles}} = \frac{n_A}{\sum n_i}$$

MASS FRACTION OF A

$$m_{fA} = \frac{\text{Mass of A}}{\text{Total mass}} = \frac{m_A}{\sum m_i}$$

PARTS PER MILLION

$$ppm = \frac{\text{Mass of substance}}{\text{Total mass}} \cdot 10^6$$

MOLARITY

$$[M] = \frac{\text{Moles dissolved solute}}{\text{Liters solution}}$$

MOLALITY

$$m = \frac{\text{Moles dissolved solute}}{\text{Kilograms solvent}}$$

CONVERSIONS

$$1 \text{ ppm} = 10^{-4} \text{ mass percent} = 10^{-6} \text{ mass fraction}$$

$$X_A = \frac{n_A}{\sum n_i} \Rightarrow \frac{n_A M_A}{\sum n_i M_i} = m_{fA} \quad \text{where: } n_A M_A = m_A, \sum n_i M_i = \sum m_i$$

$$m_{fA} = \frac{m_A}{\sum m_i} \Rightarrow \frac{m_A / M_A}{\sum m_i / M_i} = X_A \quad \text{where: } m_A / M_A = n_A, \sum m_i / M_i = \sum n_i$$

$$\text{Molarity} \times \text{Liters solution} / \text{Total moles} = X_A$$

$$\frac{\text{Molarity}}{\text{Mass fraction of solvent} \times \text{Density of solution (kg/L)}} = m$$

THE GASEOUS STATE

TEMPERATURE

$$^{\circ}\text{C (Celsius)} = 5/9(^{\circ}\text{F} - 32)$$

$$^{\circ}\text{F (Fahrenheit)} = (9/5)^{\circ}\text{C} + 32$$

$$\text{K (Kelvin)} = ^{\circ}\text{C} + 273.15$$

$$^{\circ}\text{R (Rankin)} = ^{\circ}\text{F} + 459.67$$

Examples (K)

10 ⁸	-	H-Bomb
2000	-	Bunsen burner (CH ₄ /O ₂)
1000	-	Cigarette
373	-	Boiling point of H ₂ O
310	-	Body temperature
273	-	Freezing point of H ₂ O
90	-	Boiling point of O ₂
4.2	-	Boiling point of He
0	-	Absolute zero

GAS MIXTURES

Dalton's Law of Partial Pressures

- Partial pressure, p_i , = pressure exerted by individual component at T and V of mixture

$$\sum p_i = P_{\text{total}} \quad (T, V \text{ are constant})$$

Gas 1	Gas 2	Gas 1 & 2
1 L	1 L	1 L
T, P_1	T, P_2	T, P_{Total}

Average Molar Mass of Mixture

$$M_{\text{avg}} = \sum n_i \cdot M_i / n_{\text{tot}}$$

Amagat's Law of Partial Volumes

- Partial volume, V_i , = volume occupied by individual component at T and P of mixture

$$\sum V_i = V_{\text{total}} \quad (T, P \text{ are constant})$$

Gas 1	Gas 2	Gas 1 & 2
1 L	0.8 L	1.8 L
T, P	T, P	T, P

Density of Ideal Mixture

$$d_{\text{mixture}} = P \cdot M_{\text{avg}} / RT$$

PRESSURE

$$1 \text{ atm} = 101325 \text{ Pa}$$

$$= 1.01325 \text{ bar}$$

$$= 14.6959 \text{ psi}$$

$$= 760 \text{ mm Hg}$$

$$= 760 \text{ Torr}$$

Examples (atm)

10 ⁷	-	Center of sun
10 ⁶	-	Center of earth
500-1000	-	NH ₃ synthesis
150	-	Gas cylinder
50-75	-	CH ₄ pipeline
1	-	Atmosphere
10 ⁻⁶	-	Vapor pressure of Hg
10 ⁻¹²	-	Laboratory vacuum
100 molecules/cm ³	-	(outer space)

MOLECULAR PROPERTIES

Average Molecular Velocity

$$u = (3RT/M)^{1/2}$$

$$u_{N_2} (25^{\circ}\text{C}) \cong 500 \text{ m/s}$$

of Impacts per Second on 1 m²

$$C = 1/4(N/V)u \quad (N = \# \text{ of molecules})$$

$$C_{N_2} \cong 10^{28} \text{ collisions/m}^2 \cdot \text{s} \quad (\text{at } 1 \text{ atm, } 25^{\circ}\text{C})$$

Average Distance Between Molecules = Mean Free Path

$$\lambda = [\pi D_m^2 \cdot (N/V)]^{-1}$$

$$D_m = \text{diameter of molecule}$$

$$\lambda_{N_2} (1 \text{ atm}) \cong 10^{-7} \text{ m}$$

Diffusion Coefficient

$$D = 1/3u\lambda$$

$$D_{N_2} (1 \text{ atm, } 25^{\circ}\text{C}) \cong 0.17 \text{ cm}^2/\text{s}$$

GRAHAM'S LAW OF DIFFUSION/EFFUSION

$$\frac{\text{Rate of Transport of 1}}{\text{Rate of Transport of 2}} = \sqrt{\frac{\text{Molar Mass of 2}}{\text{Molar Mass of 1}}}$$

SINGLE GASES

1 Boyle's Law $PV = \text{Constant}$ (at constant T, n)

2 Law of Charles & Gay-Lussac $V/T = \text{Constant}$ (at constant P, n)

3 Avogadro's Hypothesis At constant T and P , equal volumes of different gases contain the same number of particles
 $V/n = \text{Constant}$ (at constant T, P)

4 Ideal Gas Law $PV = nRT$ (at low P , high T)

5 Molar Volume of an Ideal Gas $V_{\text{Molar}} = 22.414 \text{ L}$ at STP (STP = 0°C, 1 atm)

6 Density of an Ideal Gas $d = PM/RT$

7 Gas Constant, R $R = 0.08206 \text{ L} \cdot \text{atm} / \text{mol} \cdot \text{K}$
 $= 82.0578 \text{ cm}^3 \cdot \text{atm} / \text{mol} \cdot \text{K}$
 $= 8.3145 \text{ J} / \text{mol} \cdot \text{K}$
 $= 8.3145 \text{ L} \cdot \text{kPa} / \text{mol} \cdot \text{K}$
 $= 1.9859 \text{ cal}(\text{I.T.}) / \text{mol} \cdot \text{K}$
 $= 0.73024 \text{ ft}^3 \cdot \text{atm} / \text{lb-mol} \cdot \text{R}$

VAN DER WAALS EQUATION FOR REAL GASES

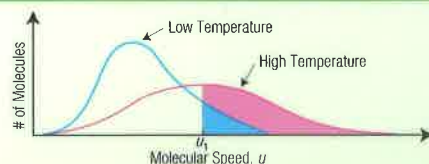
$$\left(P + \frac{an^2}{V^2} \right) (V - nb) = nRT$$

$\overbrace{\left(P + \frac{an^2}{V^2} \right)}$ pressure correction term
 $\underbrace{(V - nb)}$ volume correction term

a = measure of attractive force

b = measure of repulsive force or excluded volume

MAXWELL'S VELOCITY DISTRIBUTION OF GASEOUS MOLECULES



- As temperature increases, the average molecular speed increases, causing the curve to shift to the right and become broader

IONIC EQUILIBRIA (THE SOLUBILITY PRODUCT, K_{sp})

SPARINGLY SOLUBLE SOLIDS

- K_{sp} = Equilibrium constant of sparingly soluble ionic substances
- $$\text{Mg(OH)}_2(s) \rightleftharpoons \text{Mg}^{2+} + 2\text{OH}^-$$
- $$K_{sp} = [\text{Mg}^{2+}][\text{OH}^-]^2 = 1.2 \times 10^{-11}$$

CALCULATING ION CONCENTRATIONS

$$\text{Mg(OH)}_2 \rightleftharpoons \text{Mg}^{2+} + 2\text{OH}^-$$

$$[\text{Mg}^{2+}]/[\text{OH}^-] = 1/2 \quad \therefore [\text{Mg}^{2+}] = \frac{1}{2}[\text{OH}^-]$$

$$K_{sp} = \frac{1}{2}(\text{OH}^-)^3 = 1.2 \times 10^{-11}$$

$$\therefore [\text{OH}^-] = 2.9 \times 10^{-4} \frac{\text{mol}}{\text{L}}$$

$$[\text{Mg}^{2+}] = \frac{1}{2}[\text{OH}^-] = 1.45 \times 10^{-4} \frac{\text{mol}}{\text{L}}$$

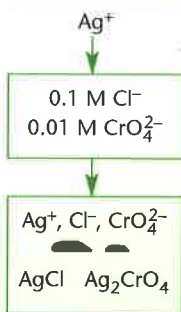
CALCULATING SOLUBILITY, s

- s = Mass of dissolved solids (g/L)
- $$\{\text{Mg(OH)}_2\}_{\text{dissolved}} \rightarrow [\text{Mg}^{2+}] = 1.45 \times 10^{-4} \frac{\text{mol}}{\text{L}}$$
- $$s = 1.45 \times 10^{-4} \times \text{Molar Mass} = 8.5 \times 10^{-3} \frac{\text{g}}{\text{L}}$$

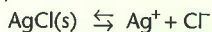
COMMON ION EFFECT

- An increase in the ion concentrations reduces the solubility (Le Chatelier)
- Solubility of Mg(OH)_2 in 1 M NaOH:
- $$[\text{Mg}^{2+}][1]^2 = 1.2 \times 10^{-11} \Rightarrow s = 7 \times 10^{-10} \frac{\text{g}}{\text{L}}$$

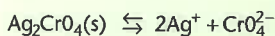
SELECTIVE PRECIPITATION



Example: Pour solution of silver ions (i.e., AgNO_3) into a beaker containing chloride and chromium anions • Which will precipitate first, AgCl or Ag_2CrO_4 ? • How complete is the separation? • Possible equilibria are:



$$K_{sp} = 2.8 \times 10^{-10}$$



$$K_{sp} = 1.9 \times 10^{-12}$$

- $[\text{Ag}^+]$ required for precipitation to start

$$[\text{Ag}^+]_{\text{AgCl}} = \frac{K_{sp}}{[\text{Cl}^-]} = \frac{2.8 \times 10^{-10}}{0.1} = 2.8 \times 10^{-9} \quad \text{AgCl precipitates first}$$

$$[\text{Ag}^+]_{\text{Ag}_2\text{CrO}_4} = \left\{ \frac{K_{sp}}{[\text{CrO}_4^{2-}]} \right\}^{1/2} = \left\{ \frac{1.9 \times 10^{-12}}{0.01} \right\}^{1/2} = 1.4 \times 10^{-5}$$

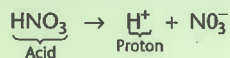
- $[\text{Cl}^-]$ remaining when Ag_2CrO_4 starts to precipitate

$$[\text{Cl}^-]_{\text{rem}} = \frac{K_{sp}}{[\text{Ag}^+]} = \frac{2.8 \times 10^{-10}}{1.4 \times 10^{-5}} = 2 \times 10^{-5} \Rightarrow 0.002\%$$

IONIC EQUILIBRIA (ACIDS & BASES)

LOWRY-BRONSTED DEFINITIONS

Bronsted Acid = Proton Donor



Bronsted Base = Proton Acceptor



ION PRODUCT OF WATER, K_w

- K_w = Dissociation equilibrium constant of water
- $$2\text{H}_2\text{O} \rightleftharpoons \text{H}_3\text{O}^+ + \text{OH}^- \quad K_w = [\text{H}_3\text{O}^+][\text{OH}^-] = 10^{-14} \quad (\text{at } 25^\circ\text{C})$$
- or
- $$\text{H}_2\text{O} \rightleftharpoons \text{H}^+ + \text{OH}^- \quad K_w = [\text{H}^+][\text{OH}^-] = 10^{-14} \quad (\text{at } 25^\circ\text{C})$$

THE pH SCALE

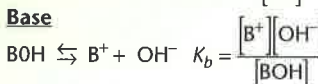
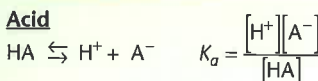
$$\text{pH} = -\log[\text{H}^+] \quad \text{pOH} = -\log[\text{OH}^-]$$

$$\text{pH} + \text{pOH} = 14 \quad (\text{at } 25^\circ\text{C})$$

- For pure water at 25°C :

$$\text{pH} = \text{pOH} = 7 \quad \text{and} \quad [\text{H}^+] = [\text{OH}^-] = 10^{-7} \frac{\text{mol}}{\text{L}}$$

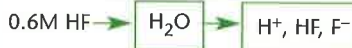
DISASSOCIATION CONSTANTS OF WEAK ACIDS & BASES



Indicators are Weak Acids or Bases



CALCULATING ION CONCENTRATIONS WITH K_a



	$\text{HF} \rightleftharpoons \text{H}^+ + \text{F}^-$	
Initial:	0.6	0
Reaction:	-X	+X
At Eq:	0.6 - X	+X

$$K_a = \frac{[\text{H}^+][\text{F}^-]}{[\text{HF}]} = \frac{X^2}{0.6 - X} = 7.1 \times 10^{-4}$$

$$X^2 + 7.1 \times 10^{-4}X - 4.32 \times 10^{-4} = 0$$

$$X = [\text{H}^+] = [\text{F}^-] = 0.021 \frac{\text{mol}}{\text{L}}$$

SOLUTIONS OF A SALT & ITS PARENT WEAK ACID OR BASE: BUFFERS

- Buffer solutions minimize changes in pH caused by addition of an acid or base
- Their pH can be calculated from the Henderson-Hasselbach equation

$$\text{pH} = \log \frac{[\text{A}^-]}{[\text{HA}]} - \log K_a$$

$$\text{pOH} = \log \frac{[\text{B}^+]}{[\text{BOH}]} - \log K_b$$

pH OF SOME FLUIDS

HCl (1M)	0.0
Vinegar	3.0
Milk	6.5
Pure water	7.0
Blood	7.4 ± 0.05
NaOH (1M)	14.0
Gastric juice	1 - 2
Lemon juice	2.4
Urine	4.8 - 7.5
Saliva	6.4 - 6.9

STRONG ACIDS & BASES (TOTAL DISSOCIATION)

HCl	LiOH
HBr	NaOH
HI	KOH
HNO_3	Ca(OH)_2
H_2SO_4	Ba(OH)_2

WEAK ACIDS & BASES (PARTIAL DISSOCIATION)

HF	NH_3
HNO_2	CH_3NH_2
HCN	$\text{C}_2\text{H}_5\text{NH}_2$
HCOOH	$\text{CO(NH}_2)_2$
CH_3COOH	$\text{C}_6\text{H}_5\text{N}$
Aspirin	Caffeine

SOLUTIONS OF SALTS OF A WEAK ACID OR BASE: HYDROLYSIS

- Salts of weak acids and bases initially dissociate completely, then hydrolyze ("split") water, resulting in a basic or acidic solution
- The hydrolysis constant can be calculated from the component K 's (i.e., K_a or K_b) and K_w



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